

# › Workbook answers

## Exercise 1.1

1

Number	Rational	Irrational
$\sqrt{36}$	✓	
$\sqrt{48}$		✓
$\sqrt{64}$	✓	
$\sqrt{84}$		✓
$\sqrt[3]{100}$		✓

2 a  $\sqrt{27}, \sqrt{500}$  b  $-36, -\sqrt[3]{8}$

- 3 a integer b surd c surd  
d integer e integer f surd

- 4 a irrational because  $\sqrt{3}$  is irrational  
b rational because it is equal to  $\sqrt{9} = 3$   
c rational because it is equal to  $8 + 4 = 12$   
d irrational because it is  $2 + \text{an irrational number}$

- 5 a 2.25  
b it is equal to 1.5  
c yes, it is equal to 4.5  
d yes, it is equal to 1.1

- 6 a  $3^3 = 27$  and  $4^3 = 64$   
b  $9^3 = 729$  and  $10^3 = 1000$   
c  $1.1^2 = 1.21$  and  $1.2^2 = 1.44$

7 Learner's own answers. For example:

- a  $\sqrt{5}$   
b a square root between  $\sqrt{36}$  and  $\sqrt{49}$   
c  $\sqrt{2}$

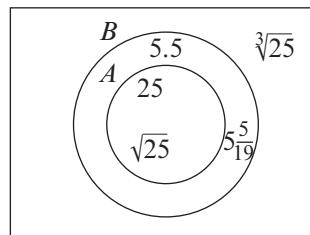
- 8 a 12 b 7

- 9 a No. All fractions are rational. In fact, the repeating sequence is nine digits long.  
b It is rational. It is  $1\frac{4}{9}$ .

- 10 a The answer is 8.  
b i  $\sqrt{2} \times \sqrt{18}$  is a possible answer.  
ii  $\sqrt{3} \times \sqrt{27}$  is a possible answer.  
iii  $\sqrt{5} \times \sqrt{20}$  is a possible answer.

- 11 a The number is 7.142... and there is no repeating pattern.  
b Learner's own answer. For example:  $\sqrt{2}$  and  $5 - \sqrt{2}$ .  
c Because the sum of two rational numbers must be rational.  
d No, because the product of two rational numbers is rational.

12



- 13 a i  $\sqrt{20} + 2 = 6.4721\dots$   
ii  $\sqrt{20} - 2 = 2.4721\dots$   
iii 16  
b She is correct. Substitute different values to see that  $(\sqrt{n} + 2)(\sqrt{n} - 2) = n - 4$  seems to be true.

## Exercise 1.2

- |                                    |                         |
|------------------------------------|-------------------------|
| 1 a $2.6 \times 10^6$              | b $9.2 \times 10^8$     |
| c $4.62 \times 10^5$               | d $2.08 \times 10^7$    |
| 2 a $5.5 \times 10^4$              | b $5.5 \times 10^7$     |
| c $6.4 \times 10^8$                | d $4.06 \times 10^8$    |
| 3 a 53 000                         | b 53 800 000            |
| c 711 000 000 000                  | d 133 100 000           |
| 4 $9.46 \times 10^{12} \text{ km}$ |                         |
| 5 a $3 \times 10^{-5}$             | b $6.66 \times 10^{-7}$ |
| c $5.05 \times 10^{-5}$            | d $4.8 \times 10^{-10}$ |
| 6 a 0.0015                         |                         |
| b 0.000 012 34                     |                         |
| c 0.000 000 079                    |                         |
| d 0.000 900 3                      |                         |
| 7 a 0.000 008                      |                         |
| b 0.000 000 482                    |                         |
| c 0.000 061                        |                         |
| d 0.000 000 070 07                 |                         |

**8**  $4 \times 10^{-7} \text{ m}$  and  $8 \times 10^{-7} \text{ m}$ **9** C, E, A, B, D**10 a** 22      **b**  $5.98 \times 10^{23} \text{ kg}$ **11 a** Copy and complete this sentence:  $6.2 \times 10^7$  is 10 times larger than  $6.2 \times 10^6$ .**b**  $10^6$  or one million.**12 a**  $4.5 \times 10^7$       **b**  $2.8 \times 10^9$ **c**  $3 \times 10^6$ **d**  $9.95 \times 10^9$ **13 a**  $4.3 \times 10^{-4}$       **b**  $1.25 \times 10^{-6}$ **c**  $7 \times 10^{-6}$ **d**  $8 \times 10^{-9}$ **14 a**  $1.75 \times 10^6$       **b**  $1.34 \times 10^8$ **c**  $6.5 \times 10^{-5}$ **d**  $1.146 \times 10^{-4}$ **Exercise 1.3**

**1 a**  $\frac{1}{7}$       **b**  $\frac{1}{49}$       **c**  $\frac{1}{125}$

**d**  $\frac{1}{81}$       **e**  $\frac{1}{225}$       **f**  $\frac{1}{400}$

**2 a**  $4^{-1}$       **b**  $4^{-3}$       **c**  $4^0$

**d**  $4^4$       **e**  $4^{-4}$       **f**  $4^{-2}$

**3 a**  $5^{-1}$       **b**  $5^2$       **c**  $5^{-2}$       **d**  $5^{-3}$       **e**  $5^0$

**4 a**  $\frac{1}{8}$       **b**  $\frac{1}{27}$   
**c**  $\frac{1}{125}$       **d**  $\frac{1}{1000}$  or 0.001

**5 a**  $12^2$       **b**  $12^{-1}$

**c**  $12^{-3}$       **d**  $12^3$

**6 a**  $5^3$       **b**  $4^{-6}$

**c**  $8^{-5}$       **d**  $15^0$  or 1

**e**  $5^{-12}$

**7 a**  $7^3$       **b**  $7^{-1}$       **c**  $7^6$       **d**  $7^{-1}$

**8 a**  $12^5$       **b**  $5^{-7}$

**c**  $3^{-4}$       **d**  $25^1$  or 25

**9 a** 6      **b** -4      **c** -2      **d** 4

**10 a** -2      **b** 4      **c** 6      **d** 7

**11 a** 3      **b**  $1\frac{3}{4}$       **c**  $1\frac{4}{9}$

**12 a**  $11^6 = 1771561$       **b**  $11^2 = 121$

**c**  $11^{-3} = \frac{1}{1331}$

**13** 7

**Exercise 2.1**

**1 a**  $2 \times x + 3 = 2 \times 10 + 3$   
 $= 20 + 3 = 23$

**b**  $x \div 2 - 4 = 10 \div 2 - 4$   
 $= 5 - 4 = 1$

**c**  $4 \times x^2 = 4 \times 10^2$   
 $= 4 \times 100 = 400$

**d**  $3 \times (x+2) = 3 \times (10+2)$   
 $= 3 \times 12 = 36$

**2** A and iii, B and v, C and i, D and vi, E and ii, F and iv

**3 a**  $x + y = 6 + -2 = 6 - 2 = 4$

**b**  $x - y = 6 - -2 = 6 + 2 = 8$

**c**  $x^2 + y^2 = 6^2 + (-2)^2 = 36 + 4 = 40$

**d**  $3x + y = 3 \times 6 + -2 = 18 - 2 = 16$

**e**  $x + 4y = 6 + 4 \times -2 = 6 - 8 = -2$

**f**  $3x + 4y = 3 \times 6 + 4 \times -2 = 18 - 8 = 10$

**4 a** 2      **b** -14      **c** 35

**d** 13      **e** 7      **f** 100

**5 a** -4      **b** 5      **c** -8

**d** -26      **e** 94      **f**  $-4\frac{1}{2}$

**g** 12      **h** -11

**6 a** Incorrect. He has worked out  $-1^2$  and not  $(-1)^2$ .

Correct solution is

$-4 \times (-1)^2 - 3 \times -4 = -4 + 12 = 8$

**b** Incorrect. He has worked out that  $(-4)^3 = 64$  and not -64.

Correct solution is  $(-4)^3 - \frac{-4}{2 \times -1} = -64 - \frac{-4}{-2}$   
 $= -64 - 2$   
 $= -66$

**7** Learner's own values. For example:**a**  $x = 3$  and  $y = 7$ ,  $x = 4$  and  $y = 44$ ,  
 $x = 5$  and  $y = 105$ **b**  $x = -1$  and  $y = -21$ ,  $x = -2$  and  $y = -28$ ,  
 $x = -3$  and  $y = -47$ **c**  $x = 0$  and  $y = -20$ ,  $x = 1$  and  $y = -19$ ,  
 $x = 2$  and  $y = -12$

- 8** a 15      b 20      c -20  
 d 11      e 8      f -64  
 g 2      h -7      i 8  
 j 2      k -25      l 4

**9** Learner's own counter-examples. For example:

- a Let  $x=2$ , so  $10x^2=10 \times 2^2=10 \times 4=40$   
 and  $(10x)^2=(10 \times 2)^2=20^2=400$   
 $40 \neq 400$ , so  $10x^2 \neq (10x)^2$ .
- b Let  $y=2$ , so  $(2y)^3=(2 \times 2)^3=4^3=64$  and  
 $2y^3=2 \times 2^3=2 \times 8=16$   
 $64 \neq 16$ , so  $(2y)^3 \neq 2y^3$ .
- c Let  $x=4$  and  $y=2$ ,  
 $3x-3y=3 \times 4-3 \times 2=12-6=6$  and  
 $3(y-x)=3(2-4)=3 \times -2=-6$   
 $6 \neq -6$ , so  $3x-3y \neq 3(y-x)$ .

- 10** a 18 kg      b 14 kg  
 c

Age (A years)	1	2	3	4	5
Mass using expression ①	10.5	13	15.5	18	20.5
Mass using expression ②	10	12	14	16	18

d Expression ②, 13.5 kg is closer to 14 kg than 15.5 kg.

- 11** a 99      b 18

$$\begin{aligned} 12 \quad & 4d^2 - \frac{100}{c^2} - 3cd - c(c-d) \\ & = 4 \times (-3)^2 - \frac{100}{5^2} - 3 \times 5 \times -3 - 5(5-(-3)) \\ & = 36 - 4 + 45 - 40 \\ & = 37 \\ & d^3 + \frac{8c}{(c+d)^2} + \left(\frac{3c}{d}\right)^2 - (-4 - c^2) \\ & = (-3)^3 + \frac{8 \times 5}{(5+(-3))^2} + \left(\frac{3 \times 5}{-3}\right)^2 - (-4 - 5^2) \\ & = -27 + 10 + 25 + 29 \\ & = 37 \end{aligned}$$

## Exercise 2.2

- |               |         |
|---------------|---------|
| <b>1</b> a 6  | b 12    |
| c $x+2$       | d $z+2$ |
| <b>2</b> a 2  | b 5     |
| c $y-3$       | d $z-3$ |
| <b>3</b> a 10 | b 20    |
| c $5a$        | d $5b$  |

- 4** a 3      b 6  
 c  $\frac{a}{5}$       d  $\frac{b}{5}$

**5** A and iii, B and vi, C and i, D and vii,  
 E and viii, F and ii, G and iv, H and v

- 6** a  $n-10$       b  $\frac{n}{1000}$   
 c  $2n+3$       d  $\frac{n}{4}-5$   
 e  $\frac{1}{n}-1$       f  $\frac{10}{2n}$   
 g  $3(n+20)$       h  $\sqrt{3n}$   
 i  $(4n)^2-3$       j  $6\sqrt[3]{n}+10$   
 k  $\left(\frac{n}{5}\right)^3-9$

- 7** a  $6x$       b  $3x+10$   
 c  $12x-2$       d  $13x-4$

- 8** a  $xy$       b  $y^2$   
 c  $x^3$       d  $16x^2$

- 9** a  $g^2=25$ ,  $g(8-g)=15$ ,  $2g(3g-11)=40$   
 b 80  
 c  $g^2+g(8-g)+2g(3g-11)=$   
 $g^2+8g-g^2+6g^2-22g=6g^2-14g$ .  
 d  $6g^2-14g=80$

- 10** a i  $2a+16$       ii  $5a+15$   
 when  $a=3$ ,  
 i  $2a+16=22$       ii  $5a+15=30$   
 b i  $2b+2$       ii  $5b-20$   
 when  $b=12$ ,  
 i  $2b+2=26$       ii  $5b-20=40$   
 c i  $4c-16$       ii  $c^2-8c$   
 when  $c=10$ ,  
 i  $4c-16=24$       ii  $c^2-8c=20$   
 d i  $2d^2+14d$       ii  $7d^3$   
 when  $d=5$ ,  
 i  $2d^2+14d=120$       ii  $7d^3=875$

- 11** a i  $2(a+3)+2(3a+1)=8a+8$ ,  
 $4(2a+2)=8a+8$   
 ii  $3(a+3)+3(3a+1)=12a+12$ ,  
 $6(2a+2)=12a+12$

**iii**  $5(a+3) + 5(3a+1) = 20a + 20$ ,  
 $10(2a+2) = 20a + 20$

**b**  $n$  black rods +  $n$  striped rods =  $2n$  white rods  
 (or similar explanation given in words)

**c i**  $4(a+3) + 2(2a+2) = 8a + 16$ ,  
 $8(a+2) = 8a + 16$

**ii**  $6(a+3) + 3(2a+2) = 12a + 24$ ,  
 $12(a+2) = 12a + 24$

**iii**  $8(a+3) + 4(2a+2) = 16a + 32$ ,  
 $16(a+2) = 16a + 32$

**d**  $2n$  black rods +  $n$  white rods =  $4n$  grey rods  
 (or similar explanation given in words)

**12 a i** \$26                                   **ii** \$46

**b** \$10   **c** \$16

**d**  $16 + 10d$

**13 a** When  $a=4$ ,  $\frac{a^2}{2} + 3a = \frac{4^2}{2} + 3 \times 4 = 20$  and  
 when  $b=5$ ,  $2b(b^2 - 4b - 3) = 2 \times 5(5^2 - 4 \times 5 - 3) = 10(25 - 20 - 3) = 20$

As the side lengths are both 20, it must be a square.

**b** 80

**c i**  $2a^2 + 12a$

**ii**  $8b^3 - 32b^2 - 24b$

**d** When  $a=4$ ,  $2a^2 + 12a = 80$  and when  $b=5$ ,  
 $8b^3 - 32b^2 - 24b = 80$

**e** Yes. Learner's own explanations.

For example: When  $a$  is a positive integer,  
 $a^2$  is positive, so  $\frac{a^2}{2}$  is positive. Also  $3a$  is positive. When you add two positive numbers, you will get a positive answer, so the perimeter of the rectangle will always be positive.

**f i** -10   **ii** -16

**iii** -18

**g** No, because the perimeter cannot be a negative number.

For  $a < -6$  the perimeter is positive, so is a valid measurement.

**14 a**  $2(4x^2 + 3x) + 2(2x^2 - 5x) =$   
 $8x^2 + 6x + 4x^2 - 10x = 12x^2 - 4x$

**b**  $12x^2 - 4x = 4x(3x - 1)$

**c** Arun is incorrect. When  $x=3$ ,  
 perimeter = 96 and when  $x=-3$   
 perimeter = 120.

**15 a** Side length =  $\sqrt[3]{27} = 3$  cm, cube has 12 edges, so total length of edges =  $12 \times 3 = 36$  cm

**b** 48 cm

**c**  $12\sqrt[3]{x}$

### Exercise 2.3

**1** A and ii, B and iv, C and i, D and iii

**2** A and iii, B and iv, C and ii, D and i

**3 a** True   **b** False  $y^5 \times y^4 = y^9$

**c** True   **d** False  $y^9 \div y^3 = y^6$

**4 a**  $g^8$    **b**  $h^{30}$

**c**  $i^{21}$    **d**  $j^{20}$

**5 a**  $8x^2$    **b**  $16x^3$

**c**  $4y^4$    **d**  $11y^6$

**6 a**  $a^7$    **b**  $b^{10}$    **c**  $c^8$

**d**  $d^4$    **e**  $e^4$    **f**  $f^7$

**g**  $g^{32}$    **h**  $y^{14}$    **i**  $i^{72}$

**j**  $13j^2$    **k**  $k^3$    **l**  $-3l^5$

**7 a**  $6a^4$    **b**  $16b^7$    **c**  $36c^{12}$

**d**  $10e^{11}$    **e**  $8g^8$    **f**  $3h^6$

**g**  $5x^8$    **h**  $5x^4$

**8 a** **B**   **b** **A**   **c** **A**   **d** **D**

**9 a** When the terms are simplified, one group has  $x^6$  terms and one group has  $x^9$  terms.

$x^6$  terms:  $3x^3 \times 2x^3$ ,  $9x^9 \div 3x^3$ ,  $2x \times 3x^5$

$x^9$  terms:  $x^6 \times 3x^3$ ,  $12x^{12} \div 4x^3$ ,  $6x^6 \times x^3$

**b**  $9x^{12} \div x^9 = 9x^3$ : this is the only card, which when simplified, has an  $x^3$  term; all others have  $x^6$  terms or  $x^9$  terms.

**10 a** Zara is correct.  $(2x^3)^2 = 2^2 \times x^{3 \times 2} = 4x^6$

**b** **i**  $9x^{14}$    **ii**  $64y^{27}$    **iii**  $32z^{15}$

**11 a** **C**   **b** **A**   **c** **B**   **d** **D**

**12 a**  $4^{-4} = \frac{1}{4^4}$    **b**  $5^{-3} = \frac{1}{5^3}$

**c**  $8^{-5} = \frac{1}{8^5}$    **d**  $x^{-4} = \frac{1}{x^4}$

**e**  $y^{-7} = \frac{1}{y^7}$    **f**  $z^{-1} = \frac{1}{z^1} = \frac{1}{z}$

**13 a**  $x^{-3} = \frac{1}{x^3}$    **b**  $y^{-4} = \frac{1}{y^4}$

**c**  $m^{-8} = \frac{1}{m^8}$    **d**  $n^{-5} = \frac{1}{n^5}$

- 14 a** A and v, B and iii, C and i, D and vii, E and ii, F and iv

- b** Any expression that simplifies to give  $\frac{5}{2y^7}$ .  
For example:  $10y^3 \div 4y^{10}$

**15**  $\frac{2n^2 \times 3n^5}{(2n^2)^3} = \frac{6n^7}{8n^6} = \frac{3n}{4}$

**16** Yes,  $\frac{6x^2 \times 3x^6 \times 2x^9}{4x^{13}} = \frac{36x^{17}}{4x^{13}} = 9x^4$  and  

$$\frac{(3x^4)^4}{3x \times x^2 \times 3x^9} = \frac{81x^{16}}{9x^{12}} = 9x^4$$

## Exercise 2.4

- 1 a**  $23 \times 34$

$\times$	20	3
30	600	90
4	80	12

$$600 + 90 + 80 + 12 = 782$$

- b**  $18 \times 42$

$\times$	10	8
40	400	320
2	20	16

$$400 + 320 + 20 + 16 = 756$$

- 2 a**  $(x+2)(x+3)$

$\times$	$x$	+2
$x$	$x^2$	+2 $x$
+3	+3 $x$	+6

$$x^2 + 2x + 3x + 6 = x^2 + 5x + 6$$

- b**  $(x+1)(x+4)$

$\times$	$x$	+1
$x$	$x^2$	+ $x$
+4	+4 $x$	+4

$$x^2 + x + 4x + 4 = x^2 + 5x + 4$$

- c**  $(x+5)(x+6)$

$\times$	$x$	+5
$x$	$x^2$	+5 $x$
+6	+6 $x$	+30

$$x^2 + 5x + 6x + 30 = x^2 + 11x + 30$$

**d**  $(x+3)(x+9)$

$\times$	$x$	+3
$x$	$x^2$	+3 $x$
+9	+9 $x$	+27

$$x^2 + 3x + 9x + 27 = x^2 + 12x + 27$$

**3 a**  $(x+5)(x-3)$

$\times$	$x$	+5
$x$	$x^2$	+5 $x$
-3	-3 $x$	-15

$$x^2 + 5x - 3x - 15 = x^2 + 2x - 15$$

**b**  $(x+6)(x-2)$

$\times$	$x$	+6
$x$	$x^2$	+6 $x$
-2	-2 $x$	-12

$$x^2 + 6x - 2x - 12 = x^2 + 4x - 12$$

**c**  $(x-7)(x+4)$

$\times$	$x$	-7
$x$	$x^2$	-7 $x$
+4	+4 $x$	-28

$$x^2 - 7x + 4x - 28 = x^2 - 3x - 28$$

**d**  $(x-8)(x+2)$

$\times$	$x$	-8
$x$	$x^2$	-8 $x$
+2	+2 $x$	-16

$$x^2 - 8x + 2x - 16 = x^2 - 6x - 16$$

**4 a**  $(x-1)(x-3)$

$\times$	$x$	-1
$x$	$x^2$	- $x$
-3	-3 $x$	+3

$$x^2 - x - 3x + 3 = x^2 - 4x + 3$$

**b**  $(x-4)(x-8)$

$\times$	$x$	-4
$x$	$x^2$	-4 $x$
-8	-8 $x$	+32

$$x^2 - 4x - 8x + 32 = x^2 - 12x + 32$$

**5** Learner's own answer.

- |                   |                  |          |                  |
|-------------------|------------------|----------|------------------|
| <b>6</b> <b>a</b> | $x^2 + 7x + 10$  | <b>b</b> | $x^2 + 2x - 8$   |
| <b>c</b>          | $x^2 - 3x - 18$  | <b>d</b> | $x^2 - 6x + 9$   |
| <b>e</b>          | $x^2 + 15x + 50$ | <b>f</b> | $x^2 - 13x + 40$ |
| <b>g</b>          | $x^2 + 5x - 50$  | <b>h</b> | $x^2 - 3x - 40$  |

- 7** **a** B    **b** A    **c** C    **d** C

**8** **1**  $(x+4)(x+3) = x^2 + 7x + 12$  Rohan had the final term incorrect – he added 4 and 3 to get 7, not multiplied 4 by 3 to get 12.

**2**  $(x+5)(x-9) = x^2 - 4x - 45$  Rohan simplified  $5x - 9x$  to be  $4x$  not  $-4x$ .

**3**  $(x-3)(x-2) = x^2 - 5x + 6$  Rohan had the final term incorrect – he multiplied  $-3$  by  $-2$  to get  $-6$ , and it should be  $+6$ .

- |                            |                |                 |                |                 |
|----------------------------|----------------|-----------------|----------------|-----------------|
| <b>9</b> <b>a</b> <b>i</b> | $a^2 + 4a + 4$ | <b>ii</b>       | $a^2 - 4a + 4$ |                 |
|                            | <b>iii</b>     | $b^2 + 8b + 16$ | <b>iv</b>      | $b^2 - 8b + 16$ |
|                            | <b>v</b>       | $c^2 + 2c + 1$  | <b>vi</b>      | $c^2 - 2c + 1$  |

**b** Learner's own answer. For example:  
The first and last terms are the same, the middle terms have different signs.

**c**  $(x+y)^2 = x^2 + 2xy + y^2$  so  
 $(x-y)^2 = x^2 - 2xy + y^2$

- |                             |            |            |            |  |
|-----------------------------|------------|------------|------------|--|
| <b>10</b> <b>a</b> <b>i</b> | $a^2 - 1$  | <b>ii</b>  | $a^2 - 16$ |  |
|                             | <b>iii</b> | $a^2 - 81$ |            |  |

**b** There is no term in  $a$ , and the number term is a square number.

- c**  $a^2 - 64$   
**d**  $a^2 - b^2$

**11**  $(x+4)(x-3) + x(5-x) = x^2 - 3x + 4x - 12 + 5x - x^2$   
 $= 6x - 12$   
 $= 6(x-2)$

- 12** **a** **i**  $x^2 + 12x + 36$

- ii**  $x^2 + 12x + 35$

**b** Learner's own answer. For example: There is a difference of 1.

- 13** **a** **i**  $x^2 + 14x + 49$

- ii**  $x^2 + 14x + 48$

**b** Learner's own answer. For example: There is a difference of 1.

**14** Learner's own answer. For example:

$(x+5)^2$  and  $(x+4)(x+6)$  giving  $x^2 + 10x + 25$  and  $x^2 + 10x + 24$

$(x+8)^2$  and  $(x+7)(x+9)$  giving  $x^2 + 16x + 64$  and  $x^2 + 16x + 63$ .

There is still a difference of 1.

- 15** **a**  $(2x+1)(3x+2) = 6x^2 + 4x + 3x + 2 = 6x^2 + 7x + 2$
- b** **i**  $12x^2 + 19x + 5$   
**ii**  $8y^2 - 14y - 15$

### Exercise 2.5

- |                   |   |          |  |
|-------------------|---|----------|--|
| <b>1</b> <b>a</b> | $\frac{1}{3} + \frac{1}{3} = \frac{2}{3}$               | <b>b</b> | $\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$                  |
| <b>c</b>          | $\frac{2}{7} + \frac{3}{7} = \frac{5}{7}$               | <b>d</b> | $\frac{1}{8} + \frac{3}{8} = \frac{4}{8} = \frac{1}{2}$    |
| <b>e</b>          | $\frac{1}{2} + \frac{2}{9} = \frac{3}{9} = \frac{1}{3}$ | <b>f</b> | $\frac{3}{10} + \frac{3}{10} = \frac{6}{10} = \frac{3}{5}$ |

- |                   |   |          |  |
|-------------------|---|----------|--|
| <b>2</b> <b>a</b> | $\frac{x}{3} + \frac{x}{3} = \frac{2x}{3}$                | <b>b</b> | $\frac{x}{5} + \frac{2x}{5} = \frac{3x}{5}$                    |
| <b>c</b>          | $\frac{2y}{7} + \frac{3y}{7} = \frac{5y}{7}$              | <b>d</b> | $\frac{y}{8} + \frac{3y}{8} = \frac{4y}{8} = \frac{y}{2}$      |
| <b>e</b>          | $\frac{m}{9} + \frac{2m}{9} = \frac{3m}{9} = \frac{m}{3}$ | <b>f</b> | $\frac{3n}{10} + \frac{3n}{10} = \frac{6n}{10} = \frac{3n}{5}$ |

- |                   |   |          |   |
|-------------------|---|----------|---|
| <b>3</b> <b>a</b> | $\frac{1}{4} + \frac{3}{8} = \frac{2}{8} + \frac{3}{8} = \frac{5}{8}$                     | <b>b</b> | $\frac{1}{3} + \frac{2}{9} = \frac{3}{9} + \frac{2}{9} = \frac{5}{9}$ |
| <b>c</b>          | $\frac{2}{3} - \frac{1}{6} = \frac{4}{6} - \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$       |          |   |
| <b>d</b>          | $\frac{11}{12} - \frac{1}{6} = \frac{11}{12} - \frac{2}{12} = \frac{9}{12} = \frac{3}{4}$ |          |   |

- |                   |                |          |                |          |               |          |                |
|-------------------|----------------|----------|----------------|----------|---------------|----------|----------------|
| <b>4</b> <b>a</b> | $\frac{5x}{8}$ | <b>b</b> | $\frac{5y}{9}$ | <b>c</b> | $\frac{p}{2}$ | <b>d</b> | $\frac{3b}{4}$ |
|-------------------|----------------|----------|----------------|----------|---------------|----------|----------------|

- |                   |                |          |                |          |                |          |                |
|-------------------|----------------|----------|----------------|----------|----------------|----------|----------------|
| <b>5</b> <b>a</b> | $\frac{x}{2}$  | <b>b</b> | $\frac{4x}{5}$ | <b>c</b> | $\frac{12}{x}$ | <b>d</b> | $\frac{6x}{7}$ |
| <b>e</b>          | $\frac{5}{4x}$ | <b>f</b> | $\frac{y}{6}$  | <b>g</b> | $\frac{2y}{9}$ | <b>h</b> | $\frac{y}{18}$ |

- |          |                 |          |                  |
|----------|-----------------|----------|------------------|
| <b>i</b> | $\frac{5}{16y}$ | <b>j</b> | $\frac{17}{24y}$ |
|----------|-----------------|----------|------------------|
- 6** **a** A, D, F all equal  $\frac{1}{4}x$  or  $\frac{x}{4}$  and B, C both equal  $\frac{1}{2}x$  or  $\frac{x}{2}$

- b** E, which equals  $\frac{1}{3}x$  or  $\frac{x}{3}$ .

- |                   |                    |          |                     |
|-------------------|--------------------|----------|---------------------|
| <b>7</b> <b>a</b> | $\frac{x+y}{2}$    | <b>b</b> | $\frac{2x+y}{6}$    |
| <b>c</b>          | $\frac{9x+y}{12}$  | <b>d</b> | $\frac{15x-y}{18}$  |
| <b>e</b>          | $\frac{7x-8y}{12}$ | <b>f</b> | $\frac{21a+4b}{28}$ |

<b>g</b> $\frac{10a+15b}{18}$ <b>i</b> $\frac{8ab-45}{36b}$	<b>h</b> $\frac{ab-35}{7b}$	<b>4</b> <b>a</b> <b>i</b> 9 <b>iii</b> $7w+d$ <b>b</b> <b>i</b> 19 <b>ii</b> 25
<b>8</b> <b>a</b> 17 <b>c</b> $17 \neq 32$ .	<b>b</b> 32	<b>5</b> <b>a</b> $A=bh$ $A=b \times h$ swap sides: $b \times h=A$ reverse the $\times$ : $b=\frac{A}{h}$ <b>b</b> $F=bg$ $F=b \times g$ swap sides: $b \times g=F$ reverse the $\times$ : $b=\frac{F}{g}$ <b>c</b> $T=mb$ $T=m \times b$ swap sides: $m \times b=T$ reverse the $\times$ : $b=\frac{T}{m}$ <b>d</b> $X=b+rt$ swap sides: $b+rt=X$ reverse the $+$ : $b=X-rt$ <b>e</b> $M=b-kn$ swap sides: $b-kn=M$ reverse the $-$ : $b=M+kn$
<b>9</b> <b>a</b> $2x+1$ <b>c</b> $3x-4$	<b>b</b> $5x+1$ <b>d</b> $3x-4$	<b>6</b> <b>a</b> <b>i</b> $D=150$ <b>b</b> $S=\frac{D}{T}, S=20$ <b>c</b> $T=\frac{D}{S}, T=5.5$
<p>Learner's own explanation. For example: She has just crossed the 2s off and not cancelled properly.</p> <p><b>d</b> <math>\frac{8x+2}{2} = \frac{2(4x+1)}{2} = \cancel{2^1}(4x+1) = 4x+1</math></p>		
<p><b>10</b> Evan is correct.</p> $\frac{7x-14}{7} + \frac{8x+6}{2} = \cancel{7^1}(x-2) + \cancel{2^1}(4x+3) =$ $x-2+4x+3 = 5x+1$		
<p><b>11</b> <b>a</b> <math>\frac{8x+24}{4} = \frac{\cancel{4^1}(2x+6)}{\cancel{4^1}} = 2x+6</math> and  <math display="block">\frac{8x+24}{4} = \frac{8^2(x+3)}{\cancel{4^1}} = 2(x+3)</math>  <b>b</b> <b>i</b> <math>2x+4</math> and <math>2(x+2)</math>  <b>ii</b> <math>3x+9</math> and <math>3(x+3)</math>  <b>iii</b> <math>6x-9</math> and <math>3(2x-3)</math>  <b>iv</b> <math>4-6x</math> and <math>2(2-3x)</math></p>		
<p><b>12</b> <b>a</b> <math>\frac{2x+3}{2}</math>  <b>c</b> <math>\frac{2x-3}{4}</math>  <b>b</b> <math>\frac{2x+3}{5}</math>  <b>d</b> <math>\frac{5-7x}{2}</math></p>		
<p><b>13</b> <b>a</b> <math>\frac{y+x}{xy}</math> or <math>\frac{x+y}{xy}</math>  <b>c</b> <math>\frac{y-x}{xy}</math>  <b>e</b> <math>\frac{5n-2m}{mn}</math>  <b>b</b> <math>\frac{d+c}{cd}</math> or <math>\frac{c+d}{cd}</math>  <b>d</b> <math>\frac{2b+a}{ab}</math> or <math>\frac{a+2b}{ab}</math>  <b>f</b> <math>\frac{3h-4g}{gh}</math></p>		
<p><b>10</b> <b>a</b> 450 m  <b>c</b> 1078 m  <b>11</b> <b>a</b> A  <b>c</b> A  <b>12</b> <b>a</b> <math>n=\frac{p+8}{3}</math>  <b>c</b> <math>n=2pw-r</math>  <b>b</b> 1303 m  <b>d</b> 1615 m  <b>b</b> B  <b>d</b> C  <b>b</b> <math>n=7(q-k)</math>  <b>d</b> <math>n=\frac{hr^2+2}{5}</math></p>		
<p><b>13</b> Arun is correct. <math>20^\circ\text{C}=68^\circ\text{F}</math> and <math>68^\circ\text{F}&gt;65^\circ\text{F}</math>.</p> <p><b>14</b> <math>F=120</math>. Learner's own explanation and working. For example:</p> <p>Use the formula <math>a=\frac{v-u}{t}</math> to find the value of <math>a</math>.  <math>\text{So } a=\frac{v-u}{t}=\frac{32-12}{5}=4</math>.</p> <p>Then use the formula <math>F=ma</math> to work out the value of <math>F</math>. So <math>F=30 \times 4=120</math>.</p>		

**15 a**  $r = \sqrt{\frac{2A}{\pi}}$       **b** 4.8 cm

**16 a**  $A = a^2 + \frac{bh}{2}$       **b**  $A = 61$

**c**  $a = \sqrt{A - \frac{bh}{2}}$       **d**  $a = 12$

**17 a** side length of the larger cube =  $2x$

**b**  $V = 9x^3$       **c**  $x = \sqrt[3]{\frac{V}{9}}$

**d** Learner's explanation and working.  
Example:

Used the formula  $x = \sqrt[3]{\frac{V}{9}}$  to work out the

value of  $x$ .  $x = \sqrt[3]{\frac{576}{9}} = 4 \text{ cm}$

Side length of larger cube is  $2 \times 4 = 8 \text{ cm}$

Area of one face of larger cube =  $8 \times 8 = 64 \text{ cm}^2$

Surface area of larger cube =  $6 \times 64 = 384 \text{ cm}^2$